Abstract—Sub-band divided ray tracing (RT) has been widely used to reproduce as reliably as possible the ultra-wideband (UWB) radio wave propagation channel in realistic indoor environments. However, its accuracy is strictly limited by the available description of the environment. Moreover, its computational complexity scales with the number of selected subbands and the number of propagation paths. In the present work, our RT tool considers not only deterministic propagation paths but also diffuse scattering components. Based on a low-complexity sub-band divided RT implementation, we propose a calibration method for indoor UWB sub-band divided RT. The method estimates the optimal material parameters, including the dielectric parameters and the scattering parameters, using channel measurements and multiobjective simulated annealing (MOSA). This calibration can improve the accuracy of sub-band divided RT in terms of the power delay profile (PDP) and the root mean square (RMS) delay spread for all test locations including those not considered by the calibration. A measurement campaign is used to verify the calibration technique.

Keywords—ray tracing (RT), low-complexity, ultra-wideband (UWB), Multiobjective simulated annealing (MOSA).

1. INTRODUCTION

In recent years, UWB technology has gained a large amount of attention and has been applied in many fields. Deep understanding of its channel characteristics is crucial for tasks, such as indoor localization and tracking [1], [2]. For UWB system, the channel characteristics vary significantly within the entire bandwidth. Deterministic sub-band divided RT technique divides the frequency range of interest into multiple subbands. RT is performed at the center frequencies of every subband. Finally all sub-band frequency responses are combined to obtain the frequency response for the full UWB bandwidth.

It is known that the accuracy of RT is related to the exact knowledge of all material parameters describing the scattering environment. Although the reflection and transmission properties of building materials can be measured at UWB frequencies, the measured dielectric values can be inhomogeneous even in the same environment because of changing temperature and humidity conditions. Therefore, it is impossible to accurately define these dielectric parameters for each building. The situation is further exacerbated when the materials are made of a mixture of unknown components. Moreover, our RT tool involves not only the specular paths but also the diffuse scattering paths. The parameters used for the scattering mechanism cannot be directly measured. Hence, the diffuse scattering model parameters must be fitted by comparing to empirical measurement data for different materials [3].

For all these reasons the approximation of the input material parameters lead to a mismatch between the simulation results of RT and empiric measurements [4]. Therefore, it is necessary to implement a calibration algorithm for these RT parameters to improve the prediction accuracy of RT. To date, the calibration of RT based on the single objective optimization has been presented, but the diffuse scattering components are not considered in [5], [6]. Due to the nonlinear combinatorial relationship between the power taps and material dielectric parameters, a simulated annealing approach is used in these works. This method provides a general optimal solution by simultaneously tuning the permittivity and conductivity of all materials to optimize the defined objective function.

In order to significantly improve the accuracy of sub-band divided RT for the UWB indoor channels, the intensively computational simulation time needs to be reduced first. This work has been done by a low-complexity sub-band divided RT, which means not only the geometric calculation but also the electromagnetic calculation needs to be performed once for all subbands [7]. The main contributions of this paper are the following:

- MOSA is a calibration algorithm to optimize the input material parameters within a given range, which refers to the dielectric and scattering parameters. The weighted sum approach is used for the proposed MOSA by projecting the multidimensional objective space into a single space.
- We separate the measurements into specular and diffuse scattering components by cross correlation and a search
and subtract algorithm.

- The accuracy of the calibrated low-complexity sub-band divided RT algorithm is verified through measurements. Even though only one pilot measurement is used for the calibration, a significant improvement of the accuracy is obtained.

II. LOW-COMPLEXITY SUB-BAND DIVIDED RT

A. RT Tool

Our RT tool is three-dimensional (3D) and the considered propagation mechanisms are line-of-sight (LOS), reflection, penetration, diffraction and diffuse scattering. Two core calculations are: (i) the geometric computation and (ii) the electromagnetic computation [8]. The propagation paths relevant at a given location can be obtained based on the geometric computation, which is related to the accurate description of the 3D environmental database and optical principles. The electromagnetic computation calculates the electric field of the propagation path in amplitude, phase and polarization relying upon the relevant propagation mechanisms and the antenna radiation patterns [9].

A detailed description of the 3D environment is required, not only dimensions of all blocks, such as walls, windows, doors, but also the material properties including the dielectric permittivity $\varepsilon_r$ and conductivity $\sigma$, the scattering coefficient $S$ and the integer $\alpha$ indicating the width of the scattering lobe. These parameters are significant for propagation mechanisms accounted in the RT tool [7], but getting the accurate values of these parameters is very difficult. In [3], some numerical results have shown that different $S$ and $\alpha$ values can greatly influence the power gain of the diffuse scattering components.

The complex dyadic reflection and penetration coefficients involved in the corresponding propagation mechanisms are obtained by Fresnel formulas, whereas diffraction coefficients are calculated by the uniform theory of diffraction (UTD) [9]. The reflection reduction factor $R$ is defined as [10]:

$$ R \equiv \sqrt{1 - S^2}, $$

which indicates the amount of energy by which perfect specular reflections are reduced due to diffuse scattering. The path direction is not modified by the penetration mechanism in our RT tool. Moreover, the penetration case is embedded into all other propagation mechanisms.

It is known that a flat wave is scattered into multiple random directions when it is interacting with a rough surface. This mechanism has been implemented in our tool based on a directive scattering model, which assumes that the scattering lobe related to the scattering tile is steered towards the direction of the specular reflection [3]. This scattering tile is determined by recursively dividing the surface until the far field condition is fulfilled [10]. The amplitude of the diffuse scattering field is evaluated based on this model, and then a uniformly distributed random phase is added to each diffuse scattering path due to the incoherent property of the scattering paths.

B. Low-complexity Sub-band Divided RT

The sub-band divided RT algorithm applied to UWB radio channels has been presented in [11], [12]. The entire UWB bandwidth $B$ is divided into $i$ equal subbands with bandwidth $B_i$, where $i \in \{1, \cdots, I\}$ and $I$ is the total number of the subbands, and $B_i \leq 500\text{MHz}$. Instead of implementing RT at one discrete frequency point as for narrowband systems, sub-band divided RT has to be performed at multiple frequencies $f_{c,i}$, which are the respective center frequencies of each subband. The computational complexity of the sub-band divided RT at one receiver (Rx) location is directly proportional to the number of subbands.

Low-complexity sub-band divided RT is introduced in [7], the basic idea of [7] is that not only the geometric computation but also the electromagnetic computation needs to be performed once at the center frequency $f_{c,i}$ of each subband $i$. Then the corresponding calculation for other subbands can be derived directly according to the physical properties of the propagation mechanisms. It is worth mentioning that distinguishing how the dielectric properties vary with frequencies is very difficult, so that it is assumed that the dielectric properties $\varepsilon_r$ and $\sigma$ do not depend on the frequency within the entire UWB bandwidth [4], [13]. With the complex electric field $\eta_{\text{RT}}(f_{c,i})$ of the propagation path at the center frequency $f_{c,i}$ of the $i$-th subband is obtained, the resulting complex electric field $\eta_{\text{RT}}(f_{c,i'})$ at all other center frequency $f_{c,i'}$ can be calculated [7]. Here, we take the single order propagation case as an example:

- LOS component:

$$ \eta_{\text{RT,los}}(f_{c,i'}) = \eta_{\text{RT,los}}(f_{c,i}) \cdot \left[ \frac{g_{\text{los}}^R(f_{c,i'})}{g_{\text{los}}^R(f_{c,i})} \right]^* \cdot \frac{f_{c,i}}{f_{c,i'}}, $$

$$ e^{j2\pi(f_{c,i'}-f_{c,i})s}, \quad (2) $$

- Reflection/penetration component:

$$ \eta_{\text{RT,yp}}(f_{c,i'}) = \eta_{\text{RT,yp}}(f_{c,i}) \cdot \left[ \frac{g_{\text{yp}}^E(f_{c,i'})}{g_{\text{yp}}^E(f_{c,i})} \right]^* \cdot \frac{f_{c,i'}}{f_{c,i}}, $$

$$ e^{-j2\pi(f_{c,i}-f_{c,i'})s}, \quad (3) $$

- Diffraction component:

$$ \eta_{\text{RT,d}}(f_{c,i'}) = \eta_{\text{RT,d}}(f_{c,i}) \cdot \left[ \frac{g_{\text{d}}^E(f_{c,i'})}{g_{\text{d}}^E(f_{c,i})} \right]^* \cdot \frac{f_{c,i}}{f_{c,i'}}, $$

$$ e^{-j2\pi(f_{c,i'}-f_{c,i})s} \cdot \left[ \frac{g_{\text{d}}^R(f_{c,i'})}{g_{\text{d}}^R(f_{c,i})} \right], \quad (4) $$

- Diffuse scattering component:

$$ \eta_{\text{RT,s}}(f_{c,i'}) = \eta_{\text{RT,s}}(f_{c,i}) \cdot \left[ \frac{g_{\text{s}}^E(f_{c,i'})}{g_{\text{s}}^E(f_{c,i})} \right]^* \cdot \frac{f_{c,i}}{f_{c,i'}}, $$

$$ e^{-j2\pi(f_{c,i'}-f_{c,i})s} \cdot \left[ \frac{g_{\text{s}}^R(f_{c,i'})}{g_{\text{s}}^R(f_{c,i})} \right], \quad (5) $$

where $s$ is the total distance between transmitter (Tx) and Rx, $c$ is the speed of light, $\theta_i$ indicates the random phase with an uniform distribution in $[0, 2\pi]$, $g_{\text{los}}^E(f_{c,i})$ and $g_{\text{los}}^R(f_{c,i})$ are the complex vectors accounting for the Tx/Rx antenna polarization.
and amplitude gains within one subband in the direction of the propagation wave. For brevity, we omit the arguments of the azimuth and elevation directions of the transmitted/received wave, because the geometrical calculation of each propagation path is identical at different subbands for one Rx location. \{ \}^* designates the complex conjugate. The detailed information can be found in [7].

III. CHANNEL MODEL CALIBRATION

Simulated annealing (SA) for single objective optimization has already been employed for RT calibration without taking diffuse scattering components into account [5], [11]. Based on our RT tool, we propose to optimize not only \( \varepsilon_r \) and \( \sigma \) but also \( S \) and \( \alpha \) for each material, which play an important role for the propagation mechanisms. It has been mentioned that the reflection component and the scattering components intimately interact with each other, so that multiobjective optimization has to be considered.

A. Distinguish Deterministic and Diffuse Scattering Components in Measurements

The search and subtract approach is a maximum likelihood method for separating the deterministic and diffuse scattering paths of channel impulse response (CIR) measurements [14]. The measurement data is available in the frequency domain, so the channel transfer function (CTF) at \( N_f \) frequency points for one Rx’s location is expressed as

\[
H_{\text{Meas}} = [H_{\text{Meas},0} \cdots H_{\text{Meas},N_f-1}]^T,
\]

where \([ \cdot ]^T\) is the transpose operator. Then the corresponding CIR is obtained as

\[
h_{\text{Meas}}(\tau) = p^T(\tau)H_{\text{Meas}},
\]

where \( p(\tau) \) is the inverse Fourier transform coefficients as

\[
p(\tau) = [e^{j2\pi f_1\tau} \cdots e^{j2\pi f_{N_f-1}\tau}]^T,
\]

where \( f_L \) denotes the lowest measured frequency and \( \Delta f \) is the measured frequency step.

In order to improve the calibration accuracy greatly, the temporal deviation in the delay domain should be removed. As a reference to the deterministic part of the channel, only the deterministic propagation paths, including reflection, penetration, diffraction components, are taken into account in RT. The propagation path delay \( \tau_{\text{RTdet},k} \) and the complex amplitude \( \eta_{\text{RTdet},k} \) of the \( k \)-th deterministic path can be calculated directly by RT. Then the CIR \( h_{\text{RTdet}}(\tau) \) at one Rx location is represented as

\[
h_{\text{RTdet}}(\tau) = \sum_{k=1}^{K} \eta_{\text{RTdet},k} \delta(\tau - \tau_{\text{RTdet},k}),
\]

where \( K \) is the total number of the deterministic paths. According to the \( k \)-th propagation path delay \( \tau_{\text{RTdet},k} \), the corresponding CIRs’ interval for the \( k \)-th path of RT and the measurement is set as \( \tau_{\text{RTdet},k} \in [\tau_{\text{RTdet},k} - 5\Delta \tau, \tau_{\text{RTdet},k} + 5\Delta \tau] \), where \( \Delta \tau \) is the delay resolution. Furthermore, the cross-correlation is obtained by

\[
R_k(\tau') = \int |h_{\text{RTdet}}(\tau')| |h_{\text{Meas}}(\tau_{\text{RTdet},k} + \tau')|d\tau',
\]

where \( | \cdot | \) denotes the absolute value. Then the \( k \)-th propagation path delay of the measurement \( \tau_{\text{Meas},k} \) is obtained by

\[
\tau_{\text{Meas},k} = \arg \max_{\tau'} \{ |R_k(\tau')| \}.
\]

In addition, the complex amplitude \( \eta_{\text{Meas},k} \) of the \( k \)-th propagation path in the measurement can be obtained as

\[
\eta_{\text{Meas},k} = \frac{p^T(\tau_{\text{Meas},k})H_{\text{Meas},k}}{ \|p\|^2_2},
\]

where \( H_{\text{Meas},k} \) is the remaining CTF after subtracting the effect of the \((k - 1)\)th deterministic peak as [14]

\[
H_{\text{Meas},k} = \begin{cases} H_{\text{Meas}} & \text{if } k = 1 \\ H_{\text{Meas},k-1} - \eta_{\text{Meas},k-1}p^*(\tau_{\text{Meas},k-1}) & \text{if } k > 1. \end{cases}
\]

Then the CIRs \( h_{\text{Meas}}(\tau) \) and \( h_{\text{Meas},k}(\tau) \) of the deterministic and diffuse scattering components can be expressed similarly as (9) and (7), respectively. In addition, the CIR of diffuse scattering components based on RT \( h_{\text{RTdet}}(\tau) \) can be calculated directly by only considering the scattering components.

B. MOSA Algorithm

Simulated annealing (SA) is derived from the physical heating of a material, where the material is critically heated and then gradually cooled until reaching a steady state [5]. It is an iterative optimization algorithm which is able to provide a sub-optimal solution for arbitrary degrees of nonlinearity [6]. In the following, \( T_0 \) is a control parameter that corresponds to the initial temperature in analogy with the physical annealing process and \( x \) is the parameter vector which needs to be optimized. The MOSA algorithm in our presented work uses the weighted sum approach to project the multidimensional parameter space into a one-dimensional space [15]. Only one prior measurement is selected in our current calibration work. The sum-weighted objective function for our case is described as

\[
f(x, \lambda_{\text{det}}, \lambda_{\text{ds}}) = \lambda_{\text{det}}f_{\text{det}}(x) + \lambda_{\text{ds}}f_{\text{ds}}(x),
\]

where the weighting factors should satisfy \( \lambda_{\text{det}} \in (0, 1) \) and \( \lambda_{\text{det}} + \lambda_{\text{ds}} = 1 \), and the objective function \( f_{\text{det}}(x) \), defined as the root mean square error between the measured and RT simulated tap powers of the deterministic paths, is calculated as

\[
f_{\text{det}}(x) = \left( \frac{1}{K} \sum_{k=1}^{K} \frac{|\eta_{\text{Meas},k}|^2 - |\eta_{\text{RTdet},k}|^2}{|\eta_{\text{Meas},k}|^2} \right)^2,
\]

where \( |\eta_{\text{Meas},k}| \) and \( |\eta_{\text{RTdet},k}| \) are the amplitudes of the propagation paths normalized by the LOS component, while the objective function \( f_{\text{ds}}(x) \), defined as the mean absolute error (MAE) between the measured and RT simulated instantaneous powers of the diffuse scattering components, is computed as

\[
f_{\text{ds}}(x) = \frac{1}{N_r} \int \left| \frac{|H_{\text{Meas},k}(\tau_{\text{ex}})|^2 - |h_{\text{RTdet},k}(\tau_{\text{ex}})|^2}{|H_{\text{Meas},k}(\tau_{\text{ex}})|^2} \right| d\tau_{\text{ex}},
\]
where $N_r$ is the number of delay points, $|\beta_{\text{meas},k}^\prime(\tau_{\text{ex}})|$ and $|\beta_{\text{RTs},k}^\prime(\tau_{\text{ex}})|$ are normalized CIRs defined over the excess delay $\tau_{\text{ex}}$. In order to get the optimal parameter vector $x$, the two objection functions need to be minimized.

The basic steps involved in the MOSA algorithm for RT calibration are illustrated as following:

1) We use the normalized objective functions (15) and (16) that are in the same numerical range, which allows to fix $\lambda_{\text{det}} = 0.5$ and $\lambda_{\text{ds}} = 0.5$ and avoid another time-consuming optimization step for these two parameters.

2) Starting with an initial parameter vector $x'$, which is selected from the literature, at an initial temperature $T_0$, the solutions of the objective functions $f_{\text{det}}(x')$ and $f_{\text{ds}}(x')$ are evaluated. The corresponding results are put into a Pareto set of solutions. The Pareto set, which is a subset of feasible points of solutions, contains all points in which at least one objective function is minimized.

3) In order to get the realistic results, the ranges of each elements are defined. A new random parameter vector $x''$ is taken from the neighborhood of $x'$ within the given ranges, and the solutions of the related objective functions are re-valuated.

4) Comparing the new solutions with all other solutions in the Pareto set, $x''$ is made as the current parameter vector and the Pareto set is updated if both objective functions are minimized as $f_{\text{det}}(x''') \leq f_{\text{det}}(x')$ and $f_{\text{ds}}(x''') \leq f_{\text{ds}}(x')$. Then the process restarts from step 6. If $x''$ is not the optimal parameter vector for both objection functions, then

$$\Delta f = f(x'', \lambda_{\text{det}}, \lambda_{\text{ds}}) - f(x', \lambda_{\text{det}}, \lambda_{\text{ds}})$$

is evaluated.

5) In order to avoid being trapped into a local minimum, the parameter vector $x''$ is accepted as the current parameter vector with the probability

$$p = \begin{cases} e^{\frac{\Delta f}{T}} & \text{if } \Delta f > 0, \\ 1 & \text{if } \Delta f \leq 0. \end{cases}$$

(18)

If $x''$ is accepted, $x''$ is made as the current parameter vector. If $x''$ is not accepted, $x'$ is retained as the current parameter vector.

6) The algorithm restarts running by selecting the referenced solutions of the objective functions corresponding to the minimum $f(x, \lambda_{\text{det}}, \lambda_{\text{ds}})$ in the Pareto set.

7) The mentioned steps repeatedly run $L$ times at the same temperature $T_0$. Then the algorithm restarts with an updated temperature, which is obtained by reducing the current temperature by a temperature factor $N_T$, where $N_T < 1$.

8) The aforementioned steps run iteratively until the pre-defined number of iterations $M$ is achieved.

IV. MEASUREMENT CAMPAIGN AND RT SETUP

A 2-D top view of the indoor scenario used for both the measurement campaign and RT is illustrated in Fig.1, where the different materials are sketched with different colors. The Rhode & Schwarz ZVA-24 vector network analyzer (VNA) was used to measure the frequency-domain UWB channel at $N_f = 7501$ frequency points over the frequency range from $f_1 = 3.1\text{GHz}$ to $f_2 = 10.6\text{GHz}$ in the Signal Processing and Speech Communication laboratory at Graz University of Technology [4]. The significant blocks are concrete walls, glass windows and metal pillars [16].

Low-complexity sub-band divided RT simulations are computed for the middle horizontal line of the grid highlighted in blue in Fig. 1. The measurements at the middle point of the horizontal line is used for the calibration. The Tx and Rx antennas in the RT simulation are dipole antennas corresponding to the antennas used in measurements. In addition, the entire UWB bandwidth $B = 7.5\text{GHz}$ is divided into $I = 15$ subbands with $B_1 = 500\text{MHz}$ each. The optimized material parameters are the elements of the parameter vector $x$

$$x = [\epsilon_{\text{con}}, \sigma_{\text{c}}, S_{\text{con}}, \epsilon_{\text{metal}}, S_{\text{metal}}, \sigma_{\text{glass}}, \epsilon_{\text{glass}}],$$

(19)

where $\epsilon$ indicates concrete and $q$ glass. The metallic block is considered as a perfect electric conductor. The conductivity of glass is $\sigma_{\text{c}} = 0.5\text{S/m}$. The involved propagation mechanisms for the calibration are LOS, reflection up to the third order, penetration, single diffraction, single bounce scattering, and scattering-reflection cases.

V. NUMERICAL RESULTS

A. Deterministic and Diffuse Scattering Paths Separation from Measurements

Based on (10), the deterministic paths in the measurements are identified such that slight time of arrival deviations of the deterministic paths can be tolerated. The precise mapping of the measured and RT simulated propagation paths can help to improve the calibration accuracy. Fig. 2 shows the normalized amplitude $|\beta_{\text{det}}|$ of the deterministic paths in measurements and low-complexity sub-band divided RT before the calibration. In order to avoid a large deviation of the power of detected paths,
a threshold of the difference between \(|h_{\text{Meas},k}|\) and \(|h_{\text{RT},k}|\) of the \(k\)-th deterministic propagation path is set to 20dB. If the difference exceeds 20dB, the \(k\)-th deterministic path is deleted. Removing the deterministic components from the measurements, the remaining diffuse scattering components are calculated as the inverse Fourier transform of \(H_{\text{Meas},k}\). The CIRs \(|h_{\text{Meas},k}()\rangle\) and \(|h_{\text{RT},k}()\rangle\) are shown in Fig. 3.

\[
\begin{align*}
4 &\leq \varepsilon_{c} \leq 9, \\
0.023 &\leq \sigma_{c} \leq 0.5, \\
0 &\leq S_{\varphi} \leq 1, \\
1 &\leq \alpha_{c} \leq 4, \\
2 &\leq \varepsilon_{g,R} \leq 8, \\
0 &\leq S_{\varphi} \leq 1, \\
1 &\leq \alpha_{g} \leq 4.
\end{align*}
\]

In Fig. 4, the solutions of objective functions related to the feasible parameter vectors are shown, and the Pareto front is given. In order to make the optimized results clear, the obtained \(f_{\text{det}}(x)\) and \(f_{\text{ds}}(x)\) are normalized by the respective minimum values. Taking the solutions in the Pareto set into consideration, one parameter vector \(x_{\text{opt}}\) is selected

\[
x_{\text{opt}} = [8.92, 0.046, 0.74, 3, 3.7, 0.32, 3].
\]

C. PDP and RMS Delay Spread Comparison

Using the parameter vector \(x_{\text{opt}}\) in low-complexity sub-band divided RT, the normalized PDPs and the RMS delay spread \(\tau_{\text{rms}}\) are compared by averaging the normalized CIRs over the horizontal 22 positions, \(R_{\text{Xdsb}}\). The results are shown in Fig. 5. It is worth mentioning that the reflection-scattering case is also considered by RT. Based on the optimized material parameters, the difference of normalized PDPs between the measurements and RT simulation is reduced by 10dB and the RMS delay spread is improved about 5ns despite only one prior measurement is used for the calibration. Moreover, it can be seen that the power of the diffuse components is increased, while the power of the deterministic components

Fig. 2. Normalized amplitude \(|h_{\text{det}}|\) of the deterministic paths in measurements and low-complexity sub-band divided RT before the calibration.

Fig. 3. Normalized CIRs \(|h_{\text{Meas},k}(\tau_{\text{ex}})|\) of the measurements and the low-complexity sub-band divided RT before the calibration considering the diffuse scattering paths only.

Fig. 4. Solutions of objective functions related to the feasible parameter vectors within the Pareto front.
are not influenced. The reasons for the remaining gap are the large dimensions of the environment which cannot be modeled absolutely accurate and the higher-order propagation mechanisms that are not considered by our RT algorithm.

VI. CONCLUSION

In this paper, we calibrated the sub-band divided RT algorithm for UWB indoor channels using the MOSA algorithm to optimize the dielectric material parameters and the scattering parameters. Our method allows the joint tuning of these parameters to reduce the mismatch between measurements and RT simulations. Firstly, a low-complexity sub-band divided RT algorithm is implemented to reduce the computational complexity. Then the deterministic and diffuse scattering paths are distinguished in measurement data relying upon cross correlation and search and subtract algorithm. The MOSA algorithm is based on the weighted sum approach, in which two objective functions are used. From the finally determined Pareto set, an optimal set of material parameters can be obtained. Based on the optimal material parameters, the differences of the normalized PDPs and the RMS delay spread between measurements and low-complexity sub-band divided RT simulation results are minimized.

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